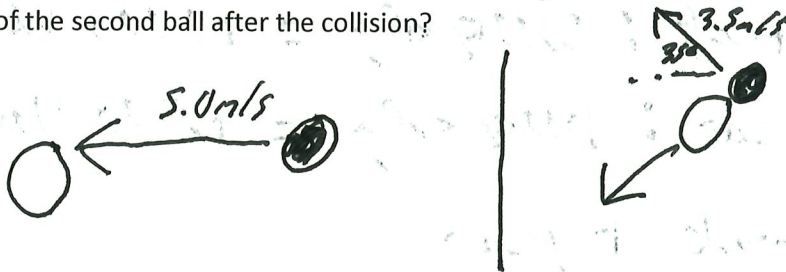




Collisions on 2D

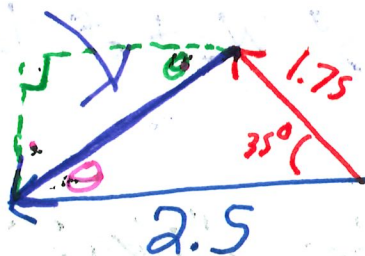
A 0.5 kg ball is travelling at 5.0 m/s to the left when it strikes a stationary 0.75 kg ball at an angle, after the collision the first ball is moving at 3.5 m/s at an angle of 35° above its original path. What is the velocity of the second ball after the collision?



$$p \text{ of first ball before collision: } 0.5 \text{ kg} \times 5.0 \text{ m/s} = 2.5 \frac{\text{kg}\cdot\text{m}}{\text{sec}} \text{ left}$$

$$p \text{ of first ball after collision: } 0.5 \text{ kg} \times 3.5 \text{ m/s} = 1.75 \frac{\text{kg}\cdot\text{m}}{\text{sec}}, 35^\circ \text{ up from left}$$

p of second ball



$$(p_2)^2 = 1.75^2 + 2.5^2 - 2(1.75)(2.5)\cos 35^\circ$$

$$p_2 = 1.4646 \frac{\text{kg}\cdot\text{m}}{\text{sec}}$$

$$\frac{\sin \theta}{1.75} = \frac{\sin 35^\circ}{1.4646} \quad \theta = 43^\circ$$

$$p_2 = 1.4646 \frac{\text{kg}\cdot\text{m}}{\text{sec}}, 43^\circ \text{ below left}$$

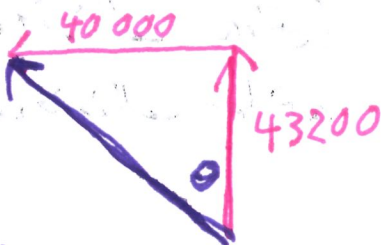
$$v = \frac{1.4646}{0.75} = 2.0 \text{ m/s}, 43^\circ \text{ below left}$$

A 2500 kg truck is travelling at 16 m/s to the West when it is struck by a 1200 kg car travelling 36 m/s North. The vehicles stick together. What is velocity of the vehicles after the collision. What kind of collision is this? What is the change in kinetic energy of the system?

$$p_{\text{initial of truck}} : 2500 \text{ kg} \times 16 \frac{\text{m}}{\text{s}} = 40000 \text{ West}$$

$$p_{\text{initial of car}} : 1200 \text{ kg} \times 36 \frac{\text{m}}{\text{s}} = 43200 \text{ North}$$

$$p_{\text{total}} = p_{\text{truck}} + p_{\text{car}}$$



$$\sqrt{40000^2 + 43200^2} \\ = 58874.78 \frac{\text{kg} \cdot \text{m}}{\text{sec}}$$

$$\tan^{-1}\left(\frac{40000}{43200}\right) = 43^\circ \text{ West of North}$$

$$\text{total mass after collision} : 2500 \text{ kg} + 1200 \text{ kg} \\ 3700 \text{ kg}$$

$$v = \frac{58874.78 \frac{\text{kg} \cdot \text{m}}{\text{sec}}}{3700 \text{ kg}} = 16 \text{ m/s}, 43^\circ \text{ West of North}$$

Perfectly inelastic

$$E_k \text{ at start} : \frac{1}{2}(2500)(16)^2 + \frac{1}{2}(1200)(36)^2 = 1097600 \text{ J}$$

$$E_k \text{ at end} : \frac{1}{2}(3700)(15.9)^2 = 467698.5 \text{ J}$$

$$\Delta E_k = 630000 \text{ J loss}$$