

Efficiency Exercises

Name: _____

1. A lightbulb takes in 62 J of electric energy and outputs 24 J of light energy. What is the efficiency of the lightbulb?

$$\text{Eff} = \frac{W_{\text{out}}}{W_{\text{in}}} = \frac{24}{62} = 0.387 \times 100\% \approx 39\%$$

2. How long will it take a 25.0 W motor with an efficiency of 65% to do 6 000 J of work?

$$P_{\text{out}} = 25 \times 0.65 = 16.25 \text{ W}$$

$$P = \frac{W}{t} \rightarrow t = \frac{W}{P} = \frac{6000}{16.25} = 369.23 \approx 370 \text{ sec}$$

3. A $5.00 \times 10^3 \text{ W}$ electric motor lifts a 200.0 kg object 5.00 m in 3.50 s. What is the efficiency of the motor?

$$P_{\text{in}} = 5000 \text{ W}$$

$$P_{\text{out}} = F \bar{v} = mg \bar{v}$$

$$= mg \frac{d}{t} = 200 \times 9.8 \times \frac{5}{3.5} = 2800 \text{ W}$$

$$\text{Eff} = \frac{P_{\text{out}}}{P_{\text{in}}} = \frac{2800}{5000}$$

$$\approx 56\%$$

4. If a 125 W motor has an efficiency of 82%, how long will it take to lift a 50.0 kg object to a height of 8.00 m?

$$P_{\text{out}} = P_{\text{in}} \times \text{Eff} = 125 \times 0.82 = 102.5 \text{ W}$$

$$P_{\text{out}} = \frac{W}{t} = \frac{\Delta E}{t} = \frac{mgh}{t} \rightarrow t = \frac{mgh}{P_{\text{out}}} = 38 \text{ sec}$$

5. An 850 kg elevator is pulled up at a constant velocity of 1.00 m/s by a 10.0 kW motor. Calculate the efficiency of the motor.

$$10 \text{ kW} = 10\,000 \text{ W}$$

$$P_{\text{out}} = F\bar{v} = mgv = 850 \times 9.8 \times 1 = 8330 \text{ W}$$

$$P_{\text{in}} = 10\,000 \text{ W}$$

$$\text{Eff} = \frac{P_{\text{out}}}{P_{\text{in}}} = \frac{8330}{10000} = 0.833 \times 100\% = \boxed{83\%}$$

6. A 2700 W heating plate is used to heat 0.80 kg of water from 20°C to 60°C in 56 seconds. [specific heat capacity of water is $4200 \frac{\text{J}}{\text{kg}^\circ\text{C}}$]

$$W_{\text{out}} = P \times t = 2700 \times 56 = 151\,200 \text{ J}$$

$$W_{\text{out}} = E_h = mc\Delta T = 0.80 \times 4200 \times 40 = 134\,400 \text{ J}$$

$$\text{Eff} = \frac{134\,400}{151\,200} = 0.89 \times 100\% = \boxed{89\%}$$

7. A 2700 W heating plate which is 56% efficient is used to heat water. How long will it take to heat 2.2 kg of water from 25°C to 100°C.

$$2700 \text{ W} \times 0.56 = 1512 \text{ W} \leftarrow \text{power out}$$

$$E_h = mc\Delta T = 2.2 \times 4200 \times 75 = 693\,000 \text{ J}$$

~~$$P = \frac{W}{t} \rightarrow t = \frac{W}{P} = \frac{693000}{1512} = 458 \text{ sec}$$~~

$$P = \frac{W}{t} \rightarrow t = \frac{W}{P} = \frac{693\,000}{1512} = 458 \text{ sec} \approx \boxed{460 \text{ sec}}$$

8. A motor is 64% efficient, how much energy does it use to move a 1300 kg car at a constant velocity of 22 m/s a distance of 750m over a surface with force of friction of 2500 N.

① How much work was done?

$$W = Fd = 2500 \times 750 = 1\,875\,000 \text{ J}$$

② $0.64 = \frac{1\,875\,000}{W_{in}} \rightarrow W_{in} = \frac{1\,875\,000}{0.64}$

$$= 2\,929\,687.5 \text{ J}$$

$$\approx (2.9 \times 10^6 \text{ J})$$

9. A motor uses 1260 J of energy to lift a 25 kg object to a height of 3.0m. What is the efficiency of the motor?

① How much work was done?

$$E_p = mgh = 25 \times 9.8 \times 3 = 735 \text{ J}$$

② $\frac{735}{1260} = 0.58 \times 100\% = (58\%)$

10. A 955.0 kg car is accelerated uniformly from rest to 16.0 m/s while moving 18.0 m across a level surface with negligible friction. If the car uses 125 000 W of power, what is the efficiency of the car?

$$P_{in} = 125000 \text{ W}$$

$$P_{out} = \frac{W}{t} \leftarrow \frac{\frac{1}{2}mv^2}{t} = \frac{122240 \text{ J}}{t}$$

$t \leftarrow \text{need to find } t$

$$V_0 = 0$$

$$V_f = 16 \text{ m/s}$$

$$d = 18$$

Use $v_f^2 = v_0^2 + 2ad$ to find a

$$a = 7.11 \text{ m/s}^2$$

Use $v_f = v_0 + at$ to find t

$$t = 2.25 \text{ sec}$$

$$P_{out} = \frac{122240}{2.25} = 54329 \text{ W}$$

$$\text{Eff} = \frac{54329 \text{ W}}{125000 \text{ W}} = 0.43 \times 100\% = 43\%$$